Name:	 		
Student ID:			

WINTER 2012 FINAL EXAM

Calculus for Electronics Engineering Technology

Dawson College: Department of Mathematics
Date: May 22nd 2012, 9:30am to 12:30pm
Course Code: 201-NYA-05 Section 6
Examiner: Emilie Richer

INSTRUCTIONS:

- All questions are to be answered directly on the examination paper in the space provided. If you need more space for your answer use the back of the page.
- SHOW ALL YOUR WORK: Show all your work clearly and justify all your answers.
- Verify that your final examination copy has a total of 19 pages including the cover page.

Question	# Marks	
1	10	
2	6	
3	5	
4	5	
5	5	
6	5	
7	5	
8	5	
9	5	
10	12	
11	10	
12	12	
13	5	
14	5	
15	5	

Question 1. (10 marks (1 mark each))

Differentiate the following functions with respect to x.

$$(a) f(x) = 4\cos(x^2)$$

(f)
$$f(x) = e^{\sin x}$$

(b)
$$f(x) = 3^x + 2x$$

(g)
$$f(x) = \ln$$

Question 2. (6 marks (1 mark each))

Integrate the following.

$$\int 4x^3 - \bar{x} \, dx$$

$$\int (2x^2 - 3)^2 dx$$

$$(c) \int 2x^3 + \cos x \, dt$$

(d)

$$\int e^x - \frac{1}{x} \, dx$$

(e)

$$\int \frac{2}{x^3} + e^{\pi} dx$$

(f)

$$\int \frac{41x^3 - 3x^2 + 1}{x} \, dx$$

Question 3. (5 marks)

Sketch a graph that satisfies all of the following conditions:

$$\lim_{x \to \infty} f(x) \quad \propto \quad$$

$$\lim_{x \to 1^+} f(x) \quad \infty$$

$$\lim_{x \to 1^{-}} f(x) - \infty$$

$$\lim_{x \to 1} f(x) = -1$$

$$f(2) = 0$$

 $\lim_{x \to 2} f(x)$ does not exist

$$f(0) = 3$$

Question 4. (5 marks)

Evaluate the following limits. If the limit does not exist, determine if its one-sided limits tend to $\pm \infty$.

(a)
$$\lim_{x \to 1} \frac{x-1}{\bar{x}-1}$$

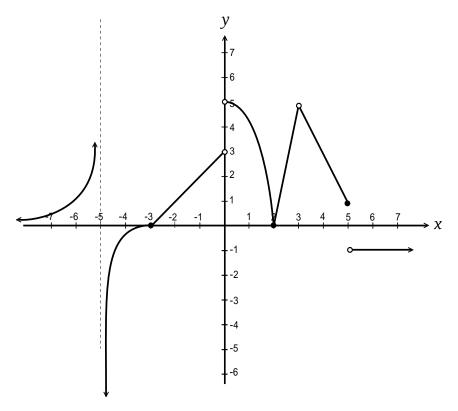
(b)
$$\lim_{x \to 1} \frac{x^2 + 3x + 2}{x^2 - 1}$$

(c)
$$\lim_{x \to \infty} \frac{x^2 + 3x^4 - 7x}{2x^3 + 2}$$

(d)
$$\lim_{x \to \infty} \frac{3x^7 - x^8 + 2}{3x^8 - 7}$$

Question 5. (5 marks)

Use the graph of y = f(x) pictured above to find the following values. If the value does not exist, write *DNE*.



(a)
$$f(0) =$$

(h)
$$\lim_{x \to \infty} f(x) =$$

(b)
$$\lim_{x \to 5^{+}} f(x) =$$

(i)
$$f(5) =$$

(c)
$$\lim_{x \to -5^{+}} f(x) =$$

(j)
$$\lim_{x \to 0^{-}} f(x) =$$

$$(d) \lim_{x \to 4} f(x) = \underline{\hspace{1cm}}$$

(k)
$$f(-1) =$$

(e)
$$\lim_{x \to \infty} f(x) = \underline{\hspace{1cm}}$$

(1)
$$\int_{-3}^{0} f(x) dx =$$

$$(f) \lim_{x \to 5} f(x) = \underline{\qquad}$$

(m)
$$\int_{5}^{7} f(x) dx =$$

(g)
$$\lim_{x \to 3^{-}} f(x) =$$

Question 6. (5 marks)

Sketch the curves $y = 2\cos x$, y = 1 and find the area between them for $0 - x - \pi$.

Question 7.(5 marks)				
Use logarithmic differentiation to find the derivative of the function $y = (\cos x)^{2x}$				
Question 8. (5 marks)				
Find the value of the constant a if the slope of the tangent line to the curve $y = -6ax^2 + 6x + 4$				
at $x = -2$ is equal to 3.				

Question 9. (5 marks)

Find the equation of the tangent line to the curve $f(x) = e^{2x} - 3x$ at the point (0,1).

Question 10. (12 marks (3 marks each))

Find the derivatives of the following functions.

(a)
$$h(t) = e^{\cos(4t)}$$

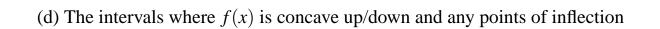
(b)
$$g(z) = 3z^{-2} \ln(\sin z)$$

(c)
$$f(x) = \log_3(\tan(x^3))$$

(d)
$$g(x) = (2x - 1)(\sin(4x))(e^{-x})$$

Question 11. (10 marks) Sketch the graph of $f(x) = x^3 - 3x$. Find and clearly identify on the sketch the following:

(a) The x $\frac{2}{3}$ \vec{n} d



SKETCH OF
$$f(x) = x^3 - 3x$$

Question 12. 12 marks (3 marks each)

Integrate the following.

(a)

$$\int \frac{-2\sin(2x)}{\cos 2x} \, dx$$

(b)
$$\int (20x^4 - 18x^2)(2x^5 - 3x^3)^{-8} dx$$

$$\int \sin^3 x \cos^2 x \, dx$$

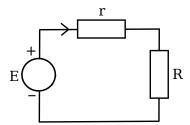
(d)
$$\int_{-1}^{4} x \ \overline{8-x} \, dx$$

Question 13. (5 marks)

A discharged ($V_c = 0$ at t = 0) 4mF capacitor is to be charged by a current of $i = 25e^{1-0.75t}$ mA. Find the capacitor voltage (V_c) at t = 135ms.

Question 14. (5 marks)

In the electric circuit shown below, the voltage E = 5 (in volts) and resistance r = 100 (in ohms) are constant, R is the resistance of a load.



In such a circuit, the electric current i is given by $\frac{E}{r+R}$ and the power P delivered to the load R is given by $P = Ri^2$.

Given that R is positive, determine the value of R so that the power P delivered to R is a maximum.

Question 15. (5 marks)

Use implicit differentiation to find the y in the following equations.

(a)
$$x^2y^3 + x + 2y = 0$$

(b) $\ln(x\sin y) + y = x^2$